

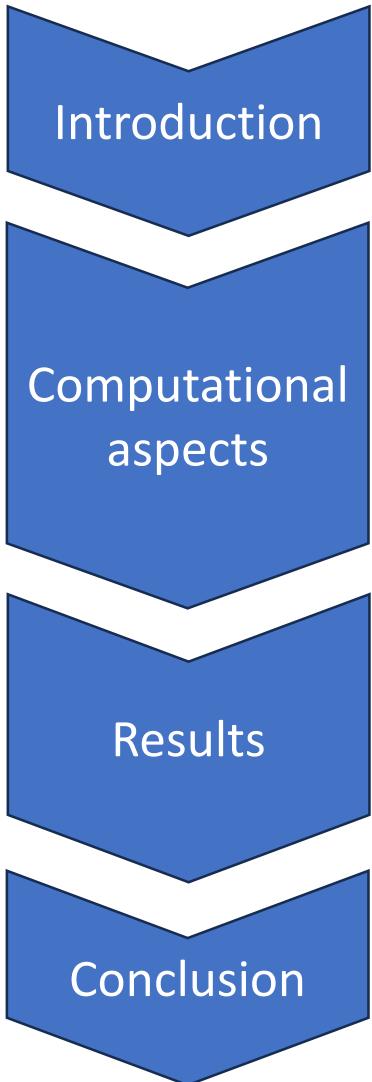
Accelerating multi-phase flow simulations with neural network models in OpenFOAM for fuel-air mixing under transcritical conditions

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Outline



- Background
- Motivation for NN
- Governing equations and thermophysical models
- CFD numerical framework
- Real-fluid data sets and NN model training
- Coupling between NN models and openFoam
- GH2-LOX test case
- Comparison between NN-version and original-version
- Performance
- Summary and Future work

Background and motivation

Context:

- Increase in energy costs
- Stringent emission policies toward climate neutrality and decarbonization

E-fuels including **hydrogen** and hydrogen carriers (**ammonia,...**) are part of the solution

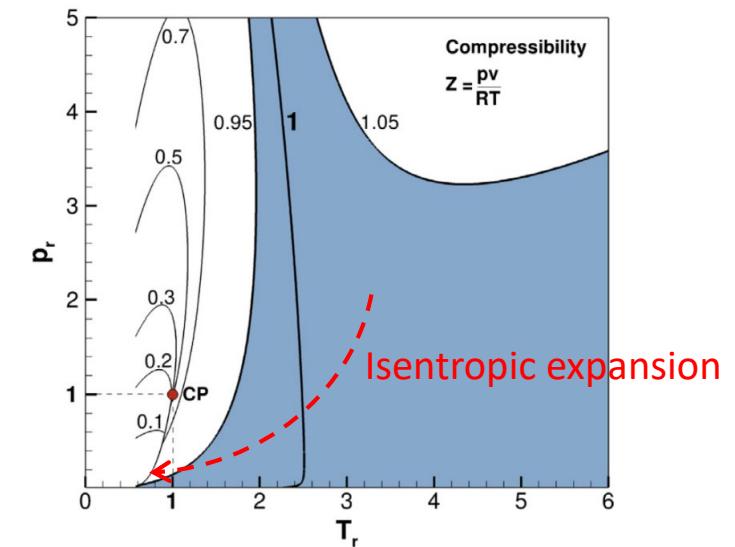


Prospectives:

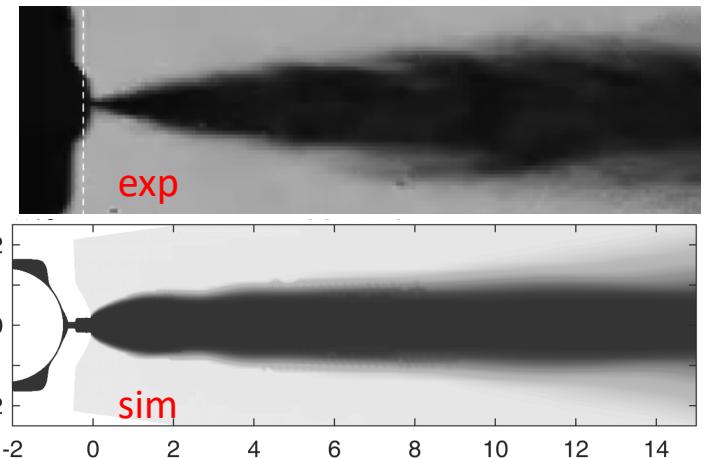
- At high-loads, heavy-duty H2-ICEs performance with DI can be comparable to FCEVs for HD transportation
- Green H2 can become a sustainable/affordable option.

Two-phase flow properties and challenges

- Accurate understanding and prediction capabilities of supercritical, and transcritical jet formation and mixing are important for clean and efficient combustion process.
- Many parameters can have large impacts (inj. pressure, back pressure, temperature, nozzle geometry)
- At high pressure, accounting for real fluids effects may be necessary
- Goal: explorations of the effect of real gas under operating conditions relevant to H₂, NH₃, other e-fuels, with high pressure, or crossing the two-phase region.



Example of ammonia flash boiling spray



Computational methods: Governing equations

- Mass

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{U}) = 0$$

τ = viscous stresses

- Momentum

$$\frac{\partial \rho \mathbf{U}}{\partial t} + \nabla \cdot (\rho \mathbf{U} \mathbf{U}) = - \nabla p + \nabla \cdot \boldsymbol{\tau}$$

q = heat flux due to conduction and species enthalpy flux

- Energy

$$\frac{\partial \rho h_T}{\partial t} + \nabla \cdot (\rho h_T \mathbf{U}) = \frac{\partial p}{\partial t} + \nabla \cdot (\mathbf{U} \cdot \boldsymbol{\tau}) - \nabla \cdot \mathbf{q}$$

- Species

$$\frac{\partial \rho Y_k}{\partial t} + \nabla \cdot (\rho Y_k \mathbf{U}) = \nabla \cdot \mathbf{J}_k$$

J_k = species diffusion velocities

- coupled with a turbulence model: RANS, LES
- diffuse interface method

Thermodynamics and transport properties

Thermodynamics

- Real-fluid mixture density ([PR EOS with non-linear Van der Waals mixing rules](#))
- Real-fluid caloric properties ([departure functions based on PR EOS for the mixture](#))

Transport

- Real-fluid transport properties ([Chung correlation](#))

- Rahamtamialisoa FNZ, et al., 2021, International Conference on Liquid Atomization and Spray Systems ILASS
- Rahamtamialisoa FNZ, et al., 2022, *Journal of Physics: Conference Series* Vol. 2385, No. 1, p. 012051. IOP Publishing.

Thermo package:

$$p(v, T, x_i) = \frac{RT}{v - b_m} - \frac{a_m}{v^2 + 2b_m v - b_m^2}$$
$$h_m(p, T) - h_{0,m}(p, T) =$$
$$= p v_m - RT + \frac{1}{2b_m\sqrt{2}} \left[a_m - T \frac{\partial a_m}{\partial T} \right] \left[\frac{v_m + b_m(1 - \sqrt{2})}{v_m + b_m(1 + \sqrt{2})} \right]$$

Mixture coefficients $a_m = \sum_i \sum_j x_i x_j a_{ij}$ $b_m = \sum_i x_i b_i$

Non-linear blends, interactions coeff., ij $a_{ij} = (1 - k_{ij})\sqrt{a_i a_j}$

| | |
|-----------------|-------------------------|
| thermoType | |
| type | hePsiThermo; |
| mixture | reactingMixture; |
| transport | chungMix; |
| thermo | janaf; |
| energy | sensibleEnthalpy; |
| equationOfState | mixturePengRobinsonGas; |
| specie | specie; |

Computational methods: Numerical frameworks

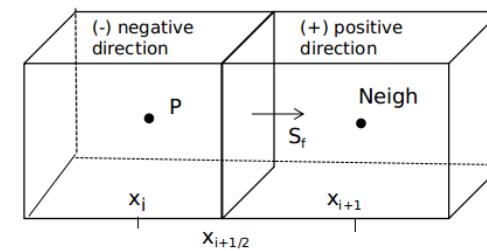
realFluidReactingFoam

- based on **reactingFoam**, with added species transport equations, and real-fluid library
- modified pressure equation to include density changes within the inner loop
- changes in the frequency of updates of other variables (enthalpy, specie)

$$\frac{\partial(\rho_0 - \psi_0 p_0)}{\partial t} + \frac{\partial \psi_0 p}{\partial t} + \frac{\partial}{\partial x_i} \left(\rho \frac{H_P}{A_P} \right) - \frac{\partial}{\partial x_i} \left(\frac{\rho}{A_P} \frac{\partial p^*}{\partial x_i} \right)$$

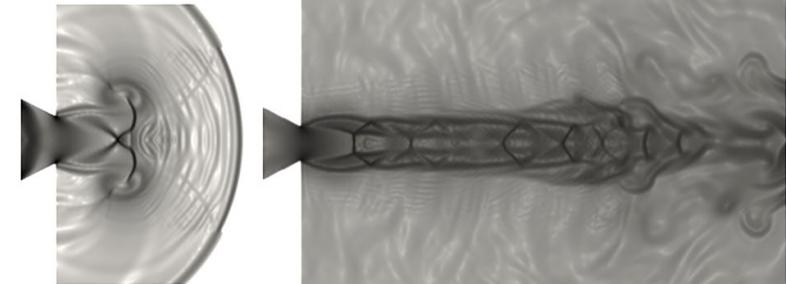
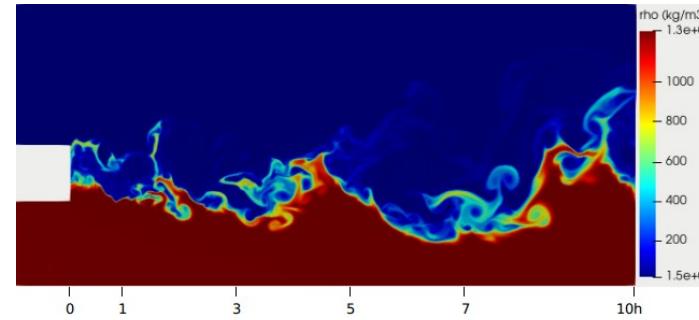
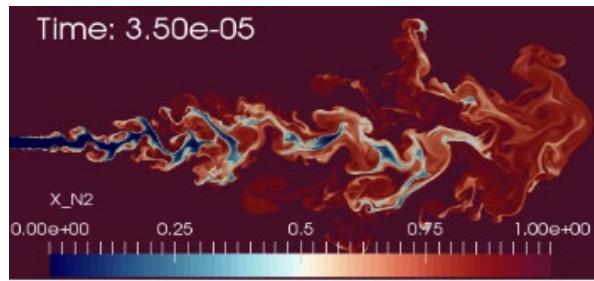
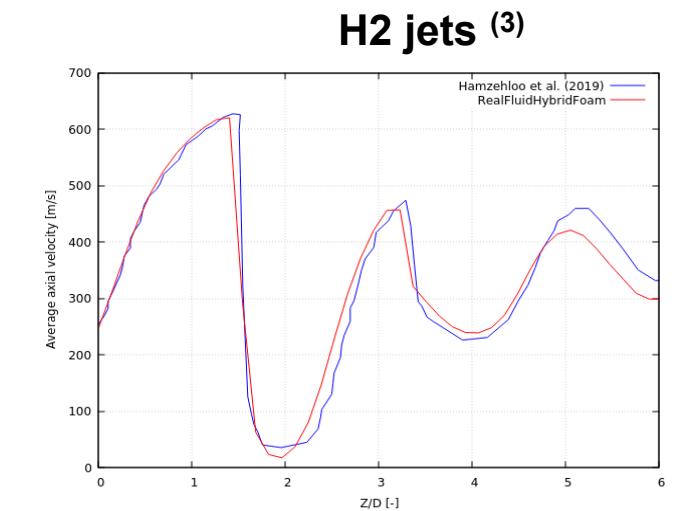
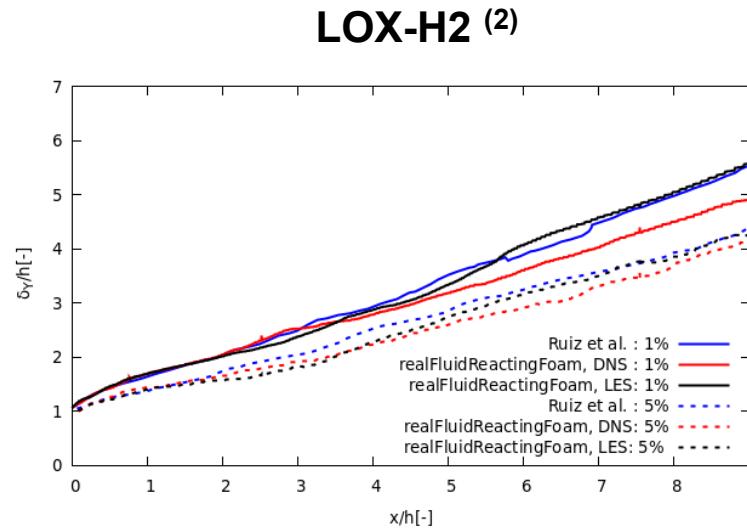
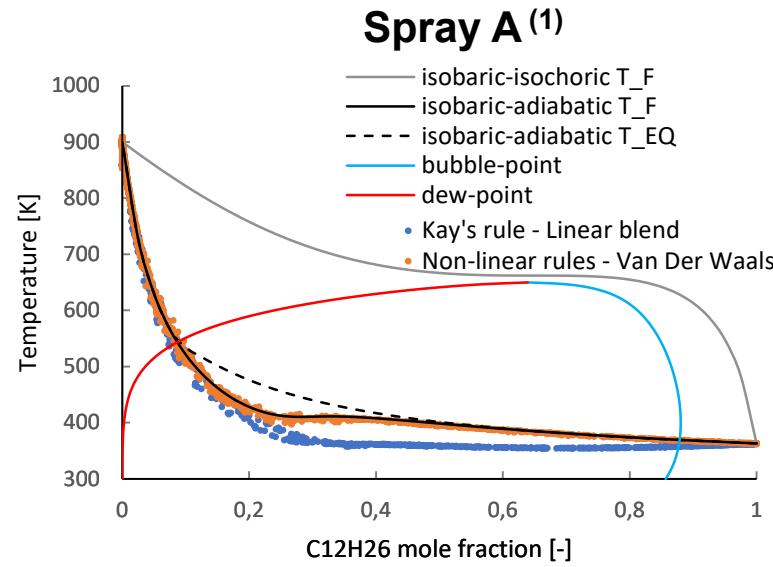
realFluidHybridFoam

- based on **rhoPimpleCentralFoam**¹, with added species transport equations, and real-fluid library
- with **KT/KNP** (Kurganov Tadmor / Kurganov Noelle Petrova) **schemes** for convective terms (flux splitting)



$$\sum_f \phi_f \Psi_f = \sum_f [\alpha \phi_{f+} \Psi_{f+} + (1 - \alpha) \phi_{f-} \Psi_{f-} + \omega_f (\Psi_{f-} - \Psi_{f+})]$$

Previous validations



¹ Ningegowda, B.M.; Rahantamialisoa, F.N.Z.; Pandal, A.; Jasak, H.; Im, H.G.; Battistoni, M.; Energies 2020, 13, 5676.

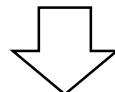
² Rahantamialisoa F.N.Z, Pandal A., Ningegowda B.M., Jacopo Z., Nasrin S., H. Jasak, Hong G. Im, Battistoni M., ICLASS 2021.

³ F Rahantamialisoa, M Battistoni, A Miliozzi, N Sahranavardfard, J Zembi, SAE Technical Paper 2023-01-0312.

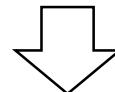
Motivation for NN

The purpose is to **reduce computational costs** of multiphase flow simulations using **neural network models** to replace heavy parts related to the calculation of the **thermophysical properties**.

A new solver, called
realFluidReactingNNFoam is derived from
realFluidReactingFoam



In this solver NN algorithm replaces real-fluid thermophysical property calculations



OpenFOAM and Python, two two different approaches

- **NNICE** ⁽¹⁾ (direct C++ inference),
- **PyFOAM** (C++ & python)

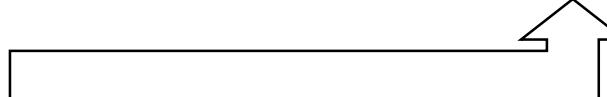
ML approach provides a speed-up factor higher than seven, while preserving the original solver accuracy ⁽²⁾



Validate the model considering liquid-oxygen (LOX) and gaseous-hydrogen (GH₂) streams



NN models use the data generated with Peng-Robinson equation of state (PR-EoS)

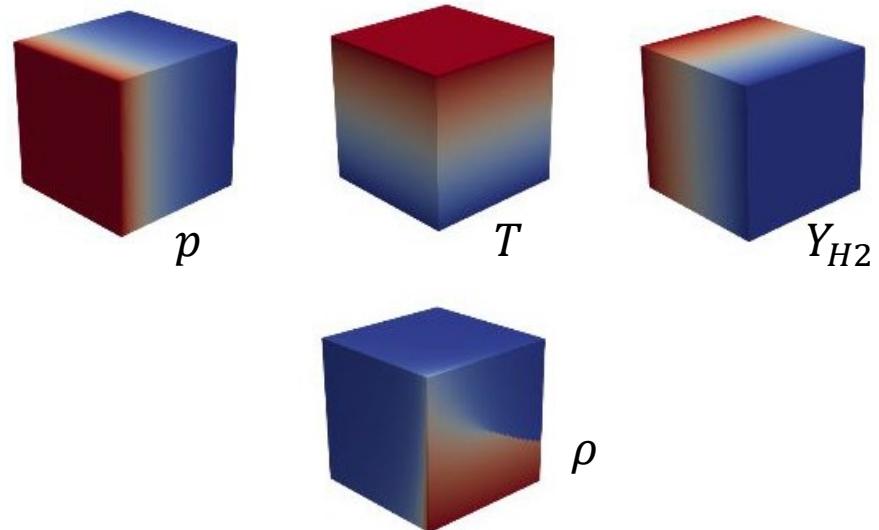


¹ D. Aubagnac (IFP-EN) <https://github.com/aubagnacd/NNICE>

² N. Sahranavardfar, D. Aubagnac-Karkar, C. Habchi, G. Costante, F. N. Z. Rahantamialisoa, and M. Battistoni. "Computation of real-fluid thermophysical properties using a neural network approach implemented in OpenFOAM", Fluids, MDPI, 2024

Real-fluid Thermophysical Data Generation

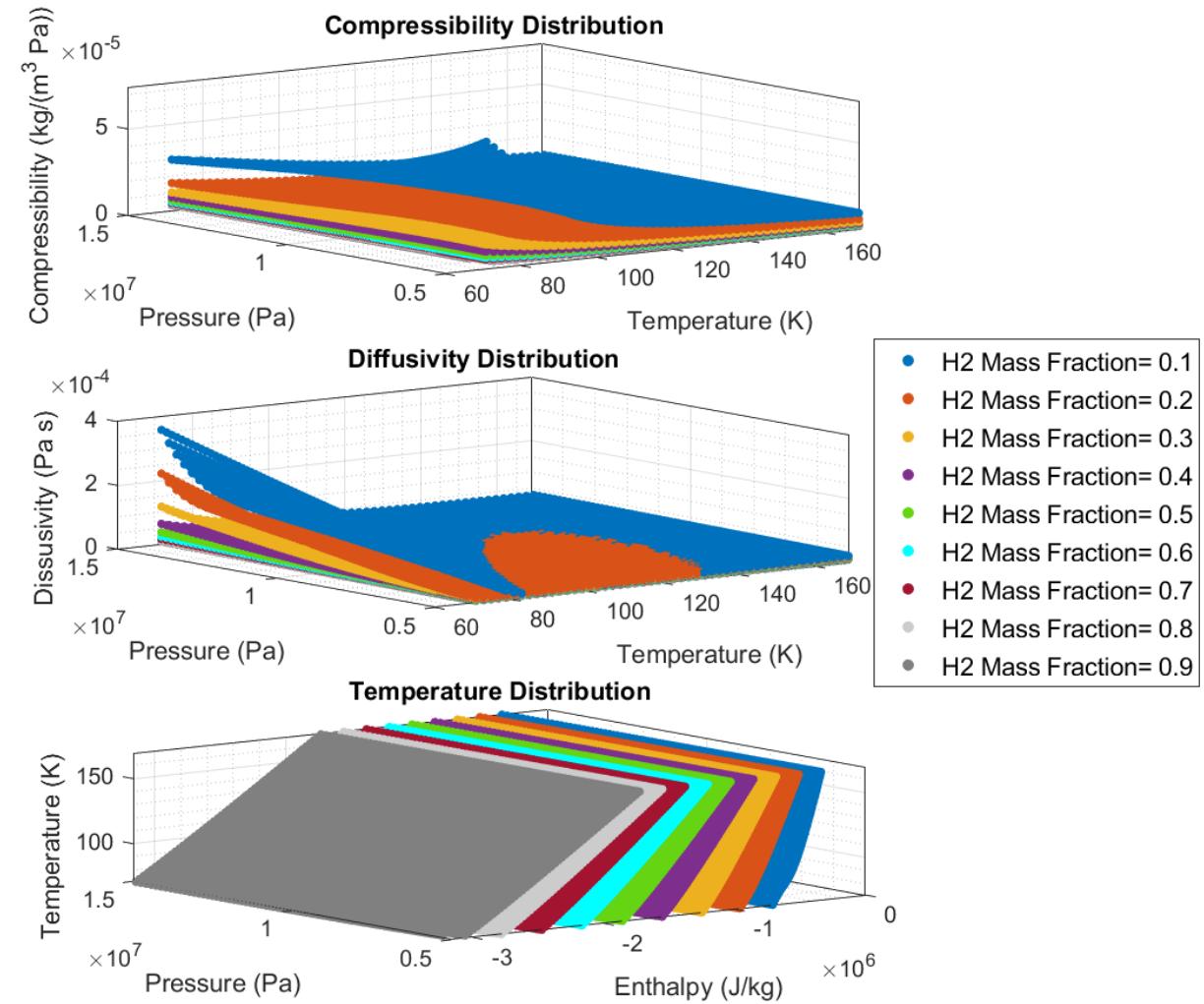
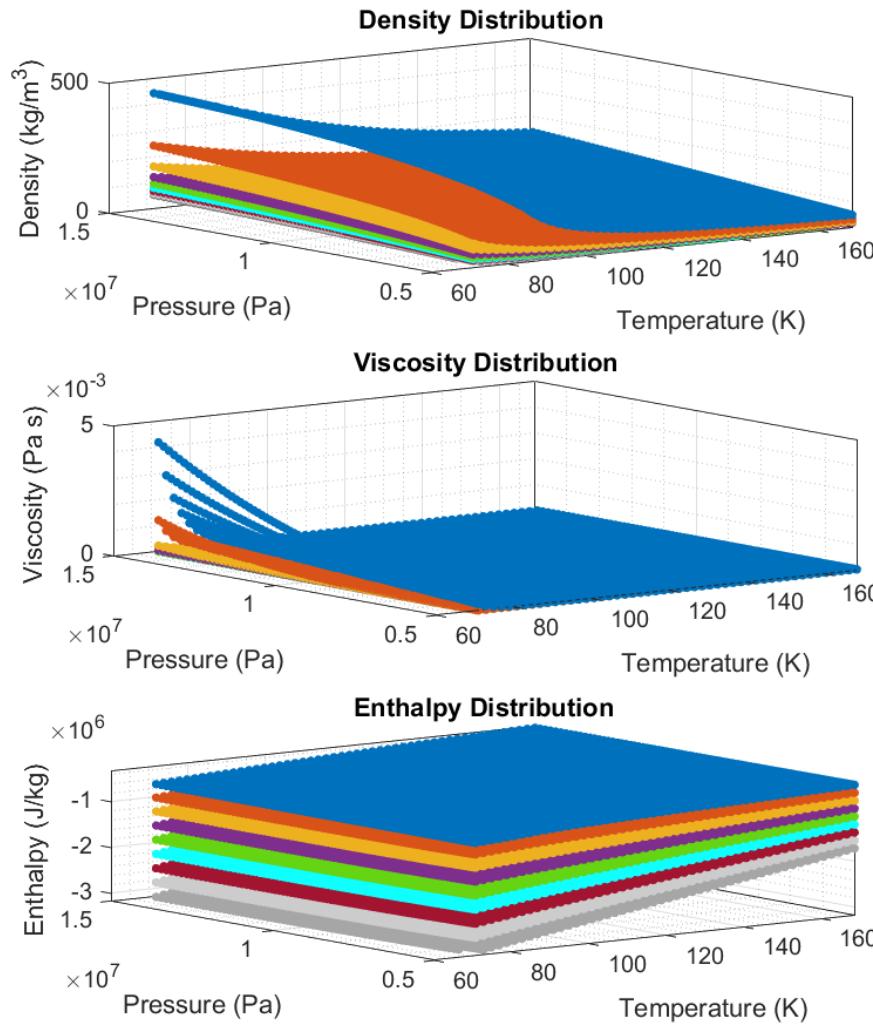
- We have three different inputs, **temperature**, **pressure**, **composition** (hydrogen mass fraction)
- Thermophysical space discretized with **250000** points.
- Data generated through
 - OpenFOAM implemented Peng-Robinson (**realFluidReactingFoam**),
 - or through IFPEN Carnot library



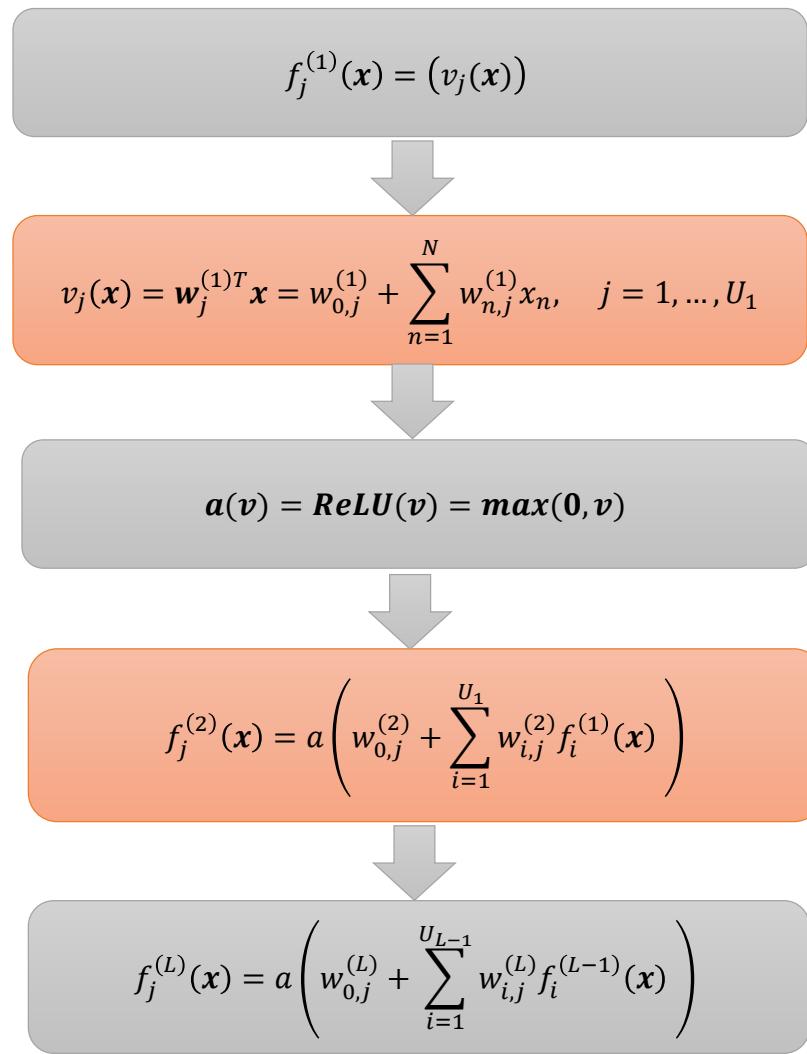
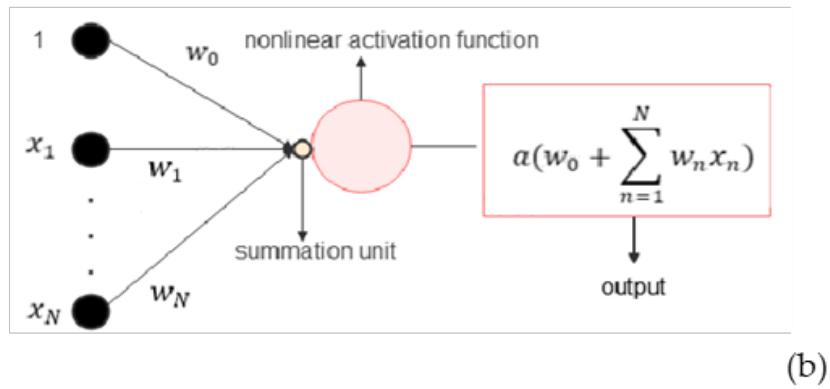
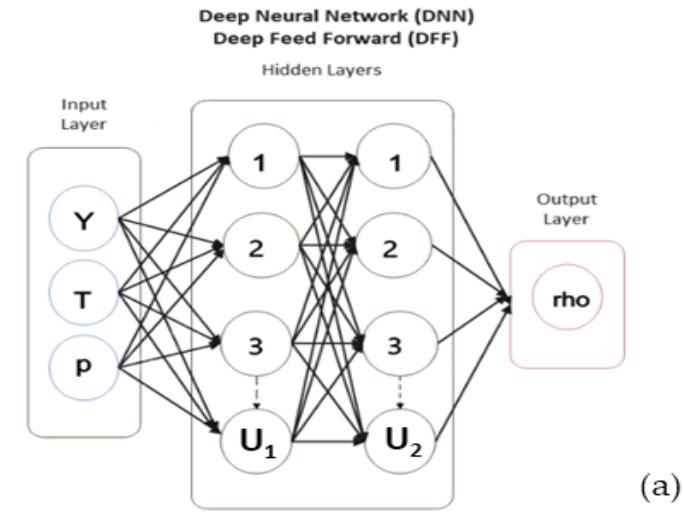
| Inputs | | Outputs |
|--------------------------------|------------------------|------------------------------------|
| Variable symbol (code name) | Definition [units] | |
| Y_{H2} (Y) | Fuel mass fraction [-] | all output variables |
| T (T) | Temperature [K] | all output variables (except T) |
| p (p) | Pressure [Pa] | all output variables |
| h (he) | Enthalpy [J/kg] | T |

| Variable symbol (code name) | Definition [units] |
|--------------------------------|--|
| ρ (rho) | Density [kg/m^3] |
| μ (mu) | Viscosity [$Pa\ s$] |
| α ($alpha$) | Thermal diffusivity [$Pa\ s$] |
| h (he) | Specific enthalpy: $h = sie + p/\rho$ [J/kg] |
| ψ (psi) | Compressibility $\psi = 1/(ZRT)$ [$kg/(m^3 Pa)$] |
| T (T) | Temperature (K) |

Thermophysical Data Visualization



NN model equations

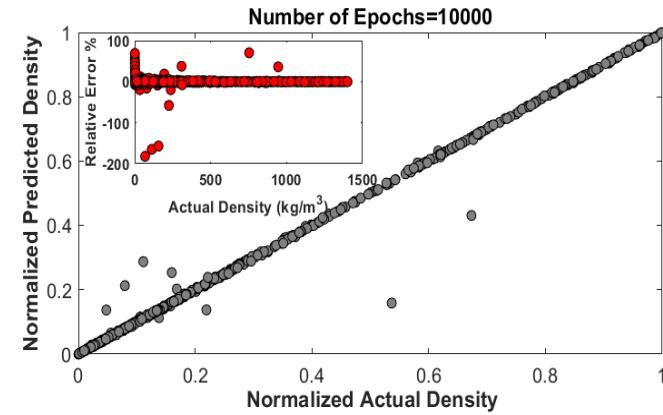
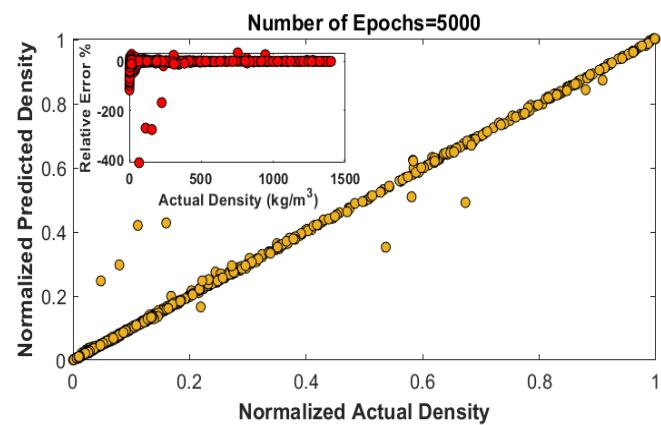
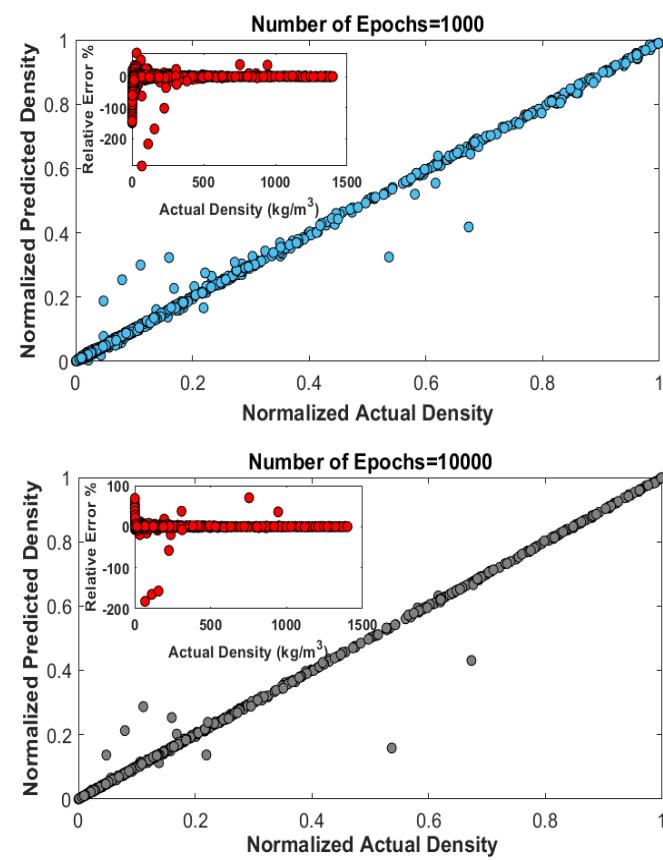
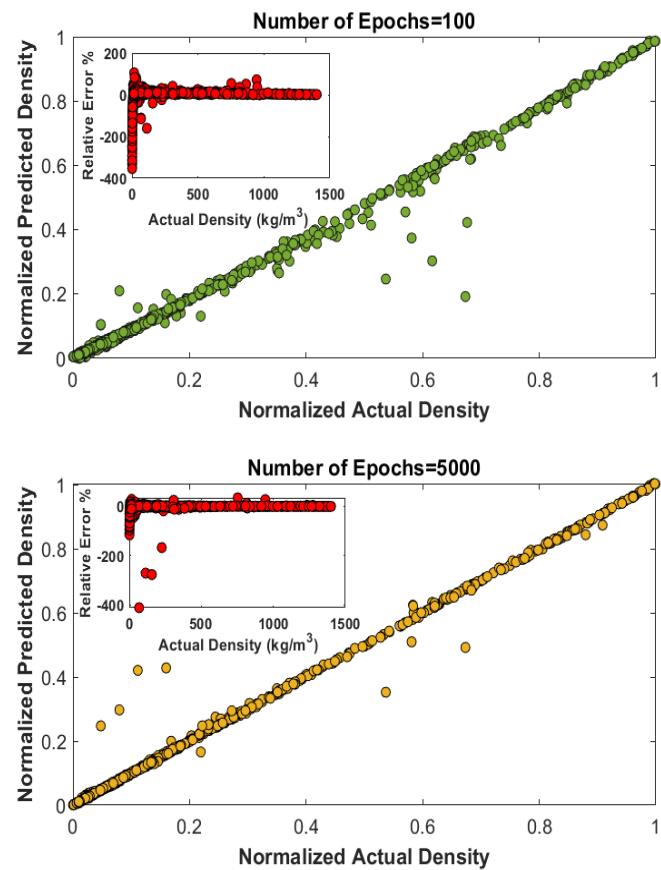
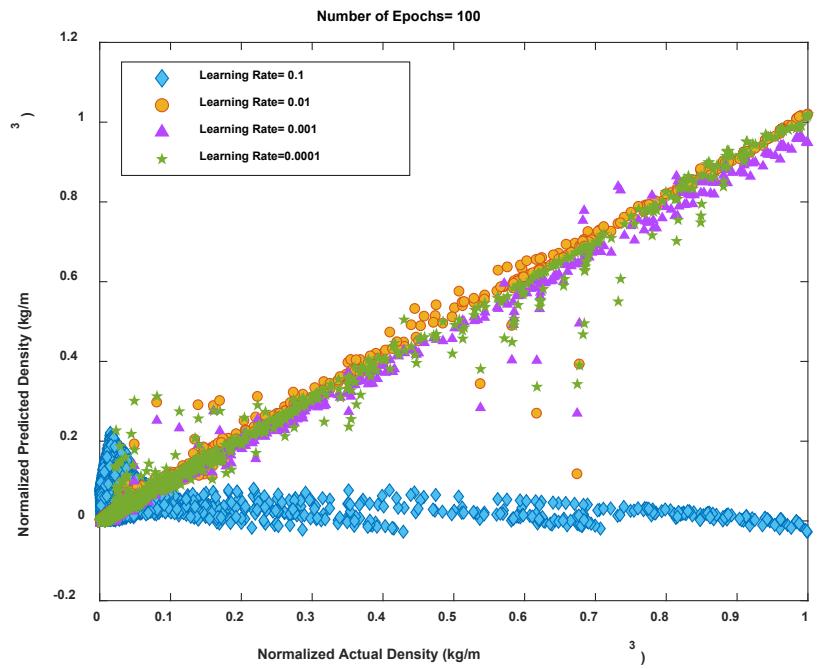


Neural Network algorithm (Python)

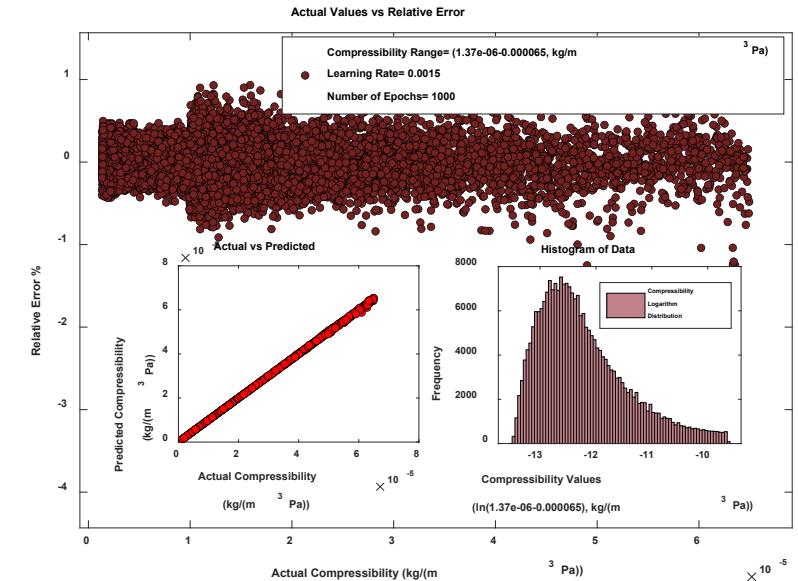
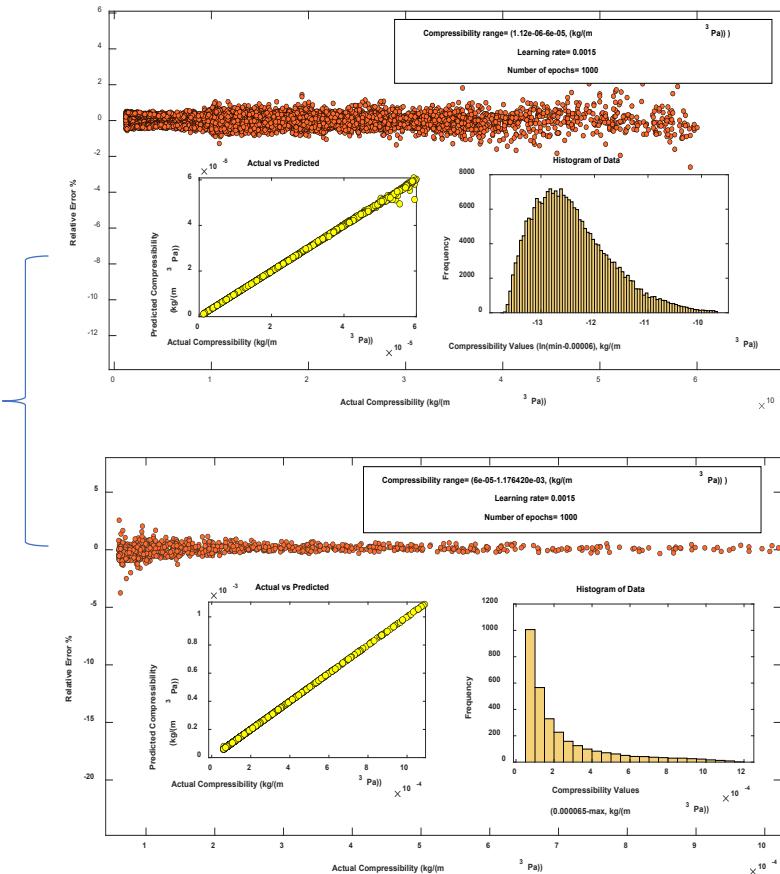
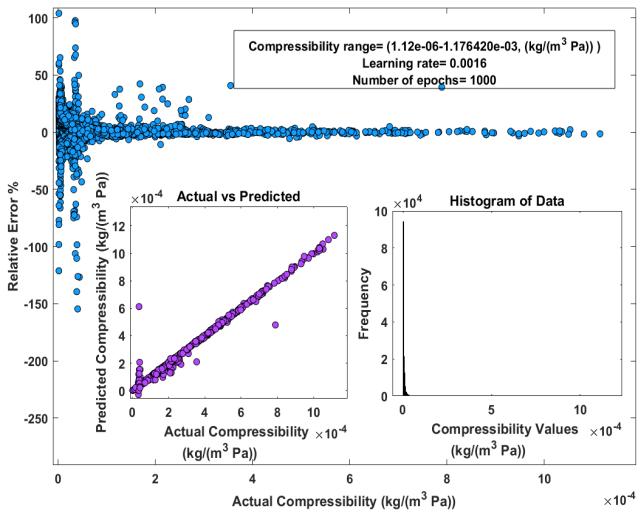
```
1 #Import Numpy and Pandas libraries as dependencies
2 import numpy as np
3 import pandas as pd
4
5 #Read data from a csv file
6 df = pd.read_csv('file.csv')
7
8 #Choose inputs and outputs from imported data
9 X = df.drop(['variable1','....','variable n'], axis=1)
10 y = df.drop(['variable1','....','variable n'], axis=1)
11
12 #Split train and test dataset, 80 percent as the trainset and 20
13 #percent as the testset
14 from sklearn.model_selection import train_test_split
15 X_train, X_test, y_train, y_test = train_test_split(X, y, test_size
16 =0.2, random_state=0)
17
18 #Transform the output data of train and test dataset
19 y_test=np.log(y_test)
20 y_train=np.log(y_train)
21
22 #Scale the input and the output data between 0 and 1
23 from sklearn.preprocessing import MinMaxScaler
24 Xscaler=MinMaxScaler(feature_range=(0,1))
25 X_train=Xscaler.fit_transform(X_train)
26 X_test=Xscaler.transform(X_test)
27 Yscaler = MinMaxScaler(feature_range=(0,1))
28 y_train=Yscaler.fit_transform(y_train)
29 y_test=Yscaler.transform(y_test)
```

```
28
29 #Import tensorflow and keras libraries, and specify the preferred
30 #hyperparameters
31 import tensorflow as tf
32 import keras
33 from keras.models import Sequential
34 from keras.layers import Dense
35 model = Sequential()
36 model.add(Dense(100, input_dim=3, activation='relu'))
37 model.add(Dense(100, activation='relu'))
38 model.add(Dense(1, activation='linear'))
39
40 #Keras optimization and the model compilation
41 lr_schedule = tf.keras.optimizers.schedules.ExponentialDecay(
42     initial_learning_rate=0.0015,
43     decay_steps=10000,
44     decay_rate=0.9)
45 opt = keras.optimizers.Adam(learning_rate=lr_schedule)
46 model.compile(loss='mse', optimizer=opt, metrics=['mae'])
47
48 #Model fit with specification of the number of epochs and the batch
49 #size
50 history = model.fit(X_train, y_train, validation_data = (X_test,
51 y_test), epochs=1000, batch_size=256)
```

Hyperparameters Importance

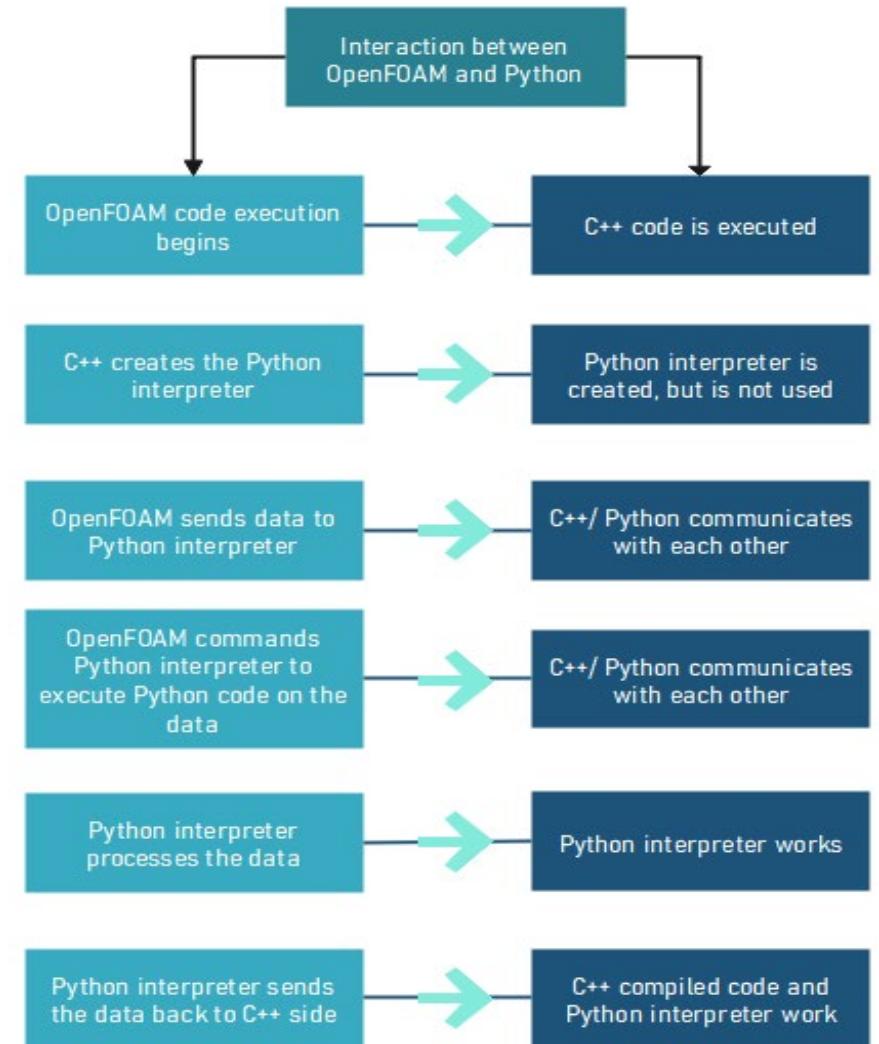
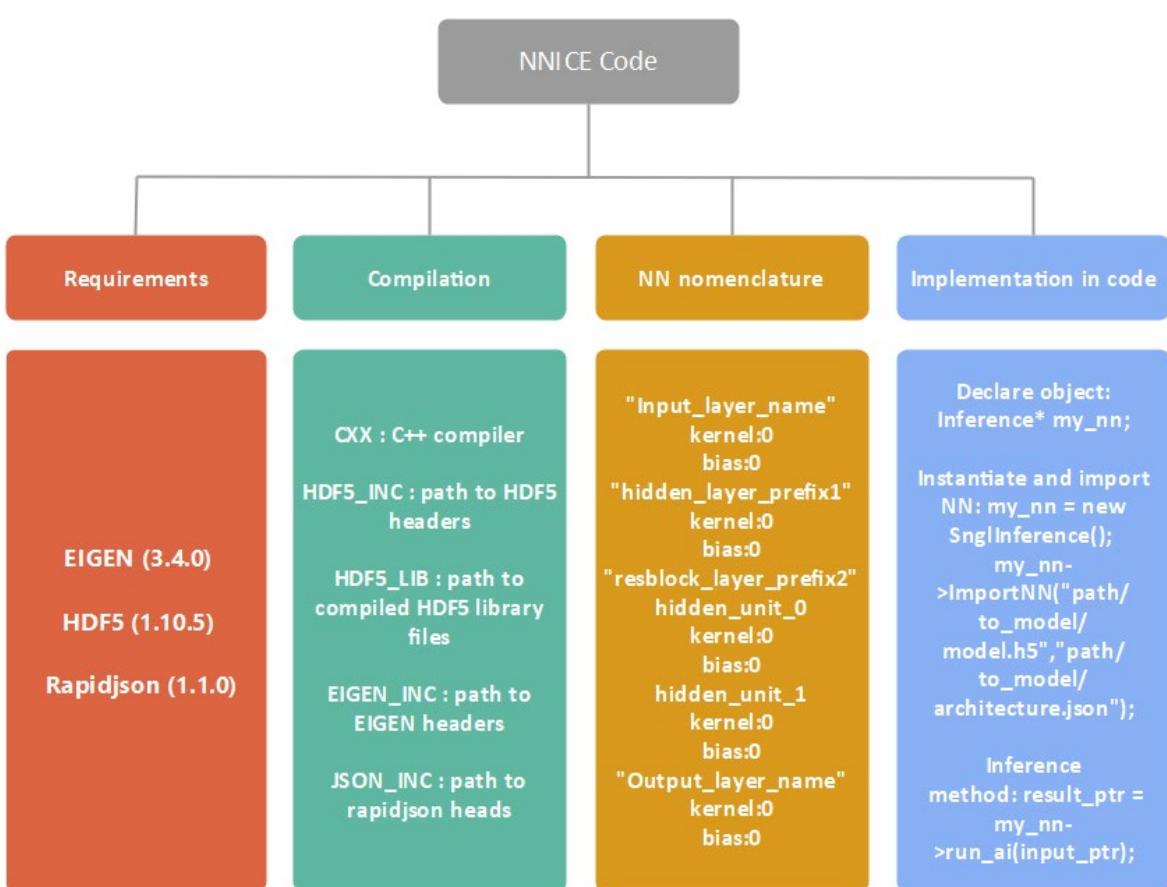


Compressibility Final Training Result

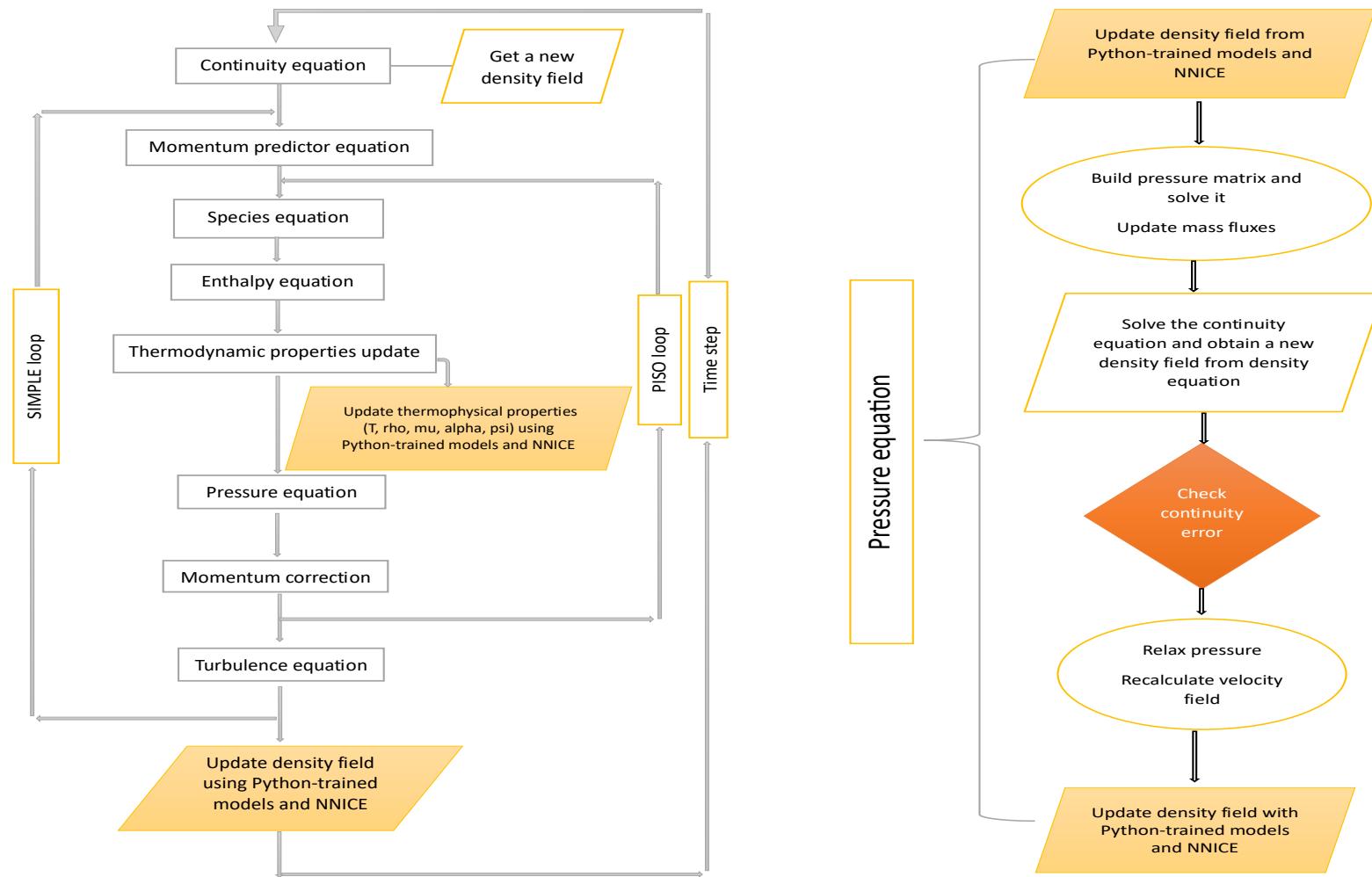


| Output (applied min-max- scalar) | Inputs (applied min-max- scalar) | Hidden layer size | Activatio- n function | Solver | Learning- rate-init | Loss metric | epoch s | batch- size |
|---|---|-------------------------|-----------------------------|--------|------------------------|----------------|------------|----------------|
| $\rho, \mu,$ $\alpha, h_e,$ $\psi,$ | Y_{H_2}, T, p | $100 \times$ 100 | ReLU | ADAM | 0.0015 | MSE | 1000 | 256 |
| T | Y_{H_2}, p, he | $100 \times$ 100 | ReLU | ADAM | 0.0015 | MSE | 1000 | 256 |

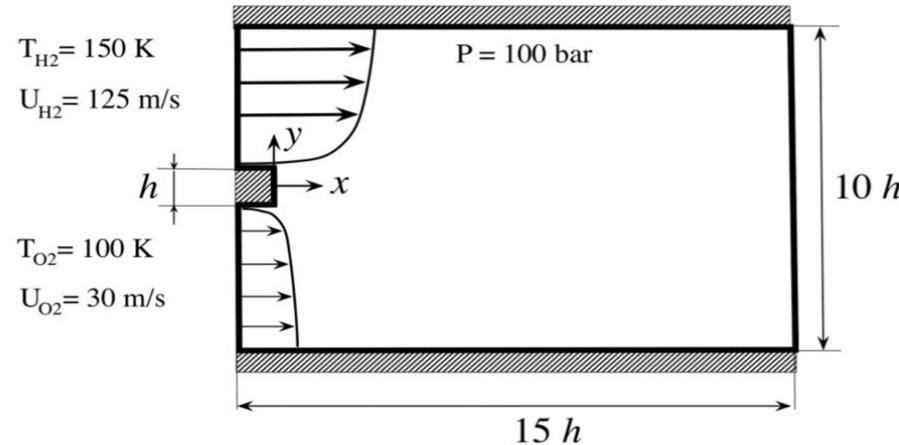
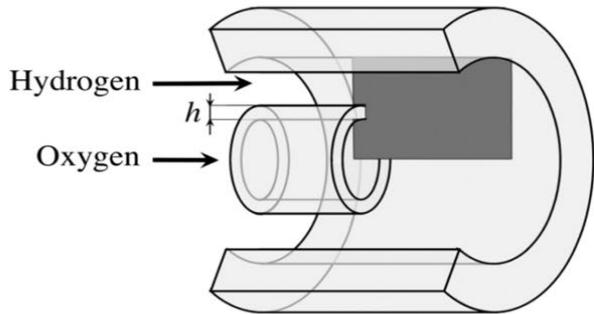
NNICE and PythonFOAM Implementations



Implementation of the NN models within the PIMPLE loop



GH2-LOX test case: operating condition

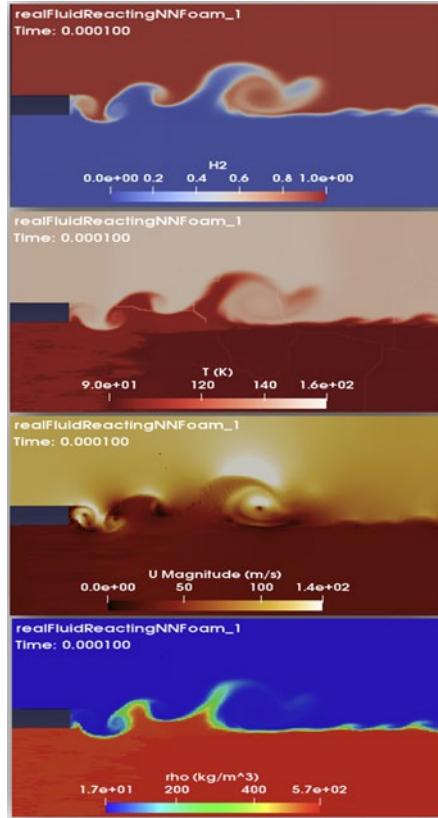


- we analyze a **two-dimensional mixing layer** with an injector lip that divides streams of liquid oxygen (**LOX**) and gaseous hydrogen (**GH2**), both at **supercritical pressure**.
- The simulation setup involves an injector lip with a height (**h**) of **0.5 mm**, segregating high-speed gaseous hydrogen (GH2) in the surroundings from dense liquid oxygen (LOX) in the center.
- The area of interest of the computational domain spans **15h** along the axial direction and **10h** in the transversal direction.
- a relatively coarse mesh is employed with a uniform grid spacing of $\Delta x/h = \Delta y/h = 20$.
- At the injector lip, we implement an **adiabatic no-slip** wall condition, while the top and bottom boundaries are treated as **adiabatic slip walls**. Furthermore, we apply a **Dirichlet pressure boundary condition** at the outlet.

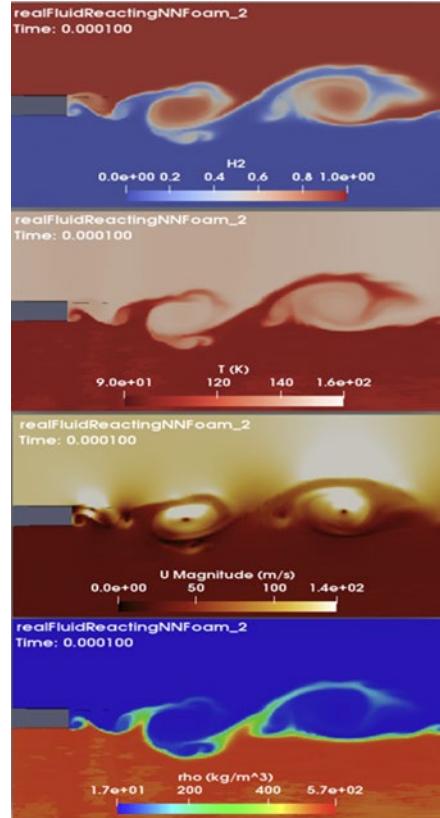
Rahantamialisoa F.N.Z., Pandal A., Ningegowda B.M., Jacopo Z., Nasrin S., H. Jasak, Hong G. Im, Battistoni M., ICLASS 2021.

GH2-LOX - Results and discussion: fields @ t = 0.1 ms

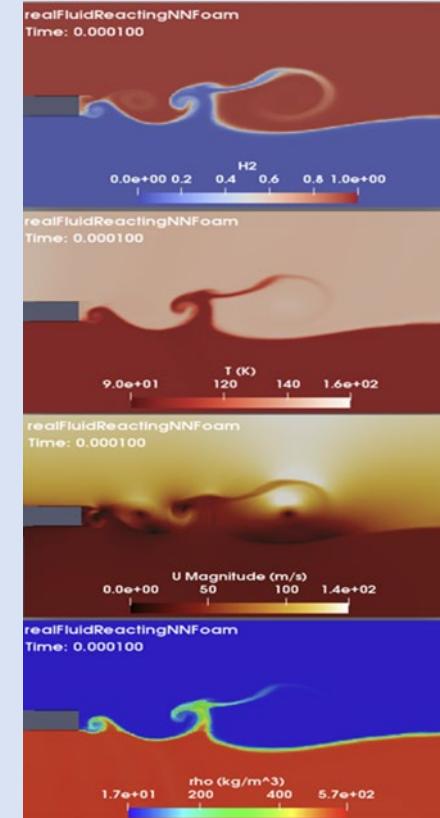
realFluidReactingNNFoam_1
NN_1



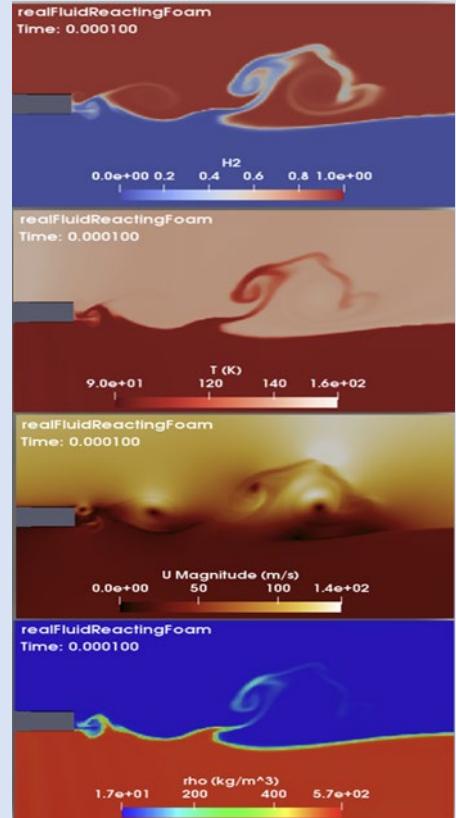
realFluidReactingNNFoam_2
NN_2



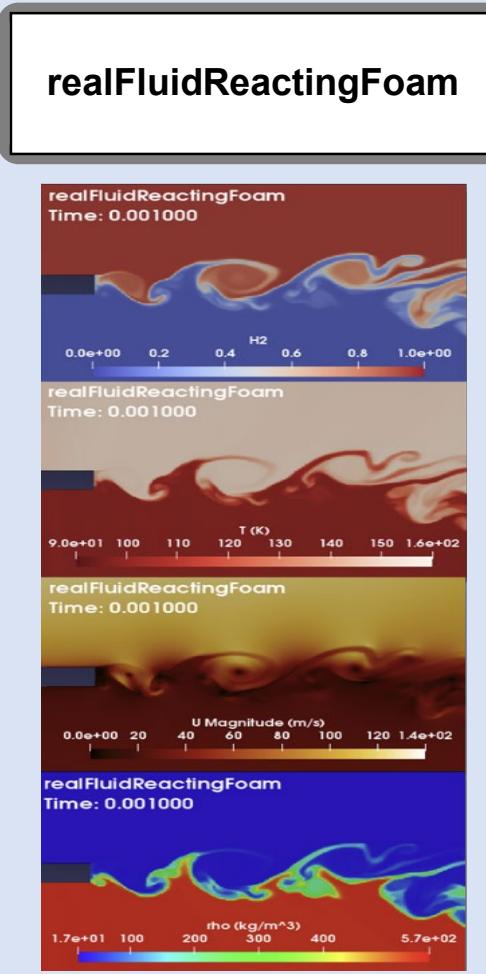
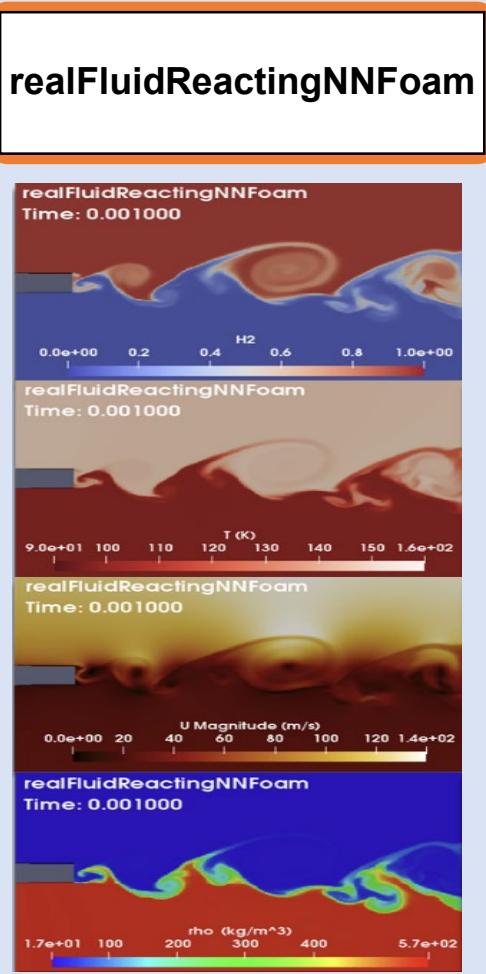
realFluidReactingNNFoam



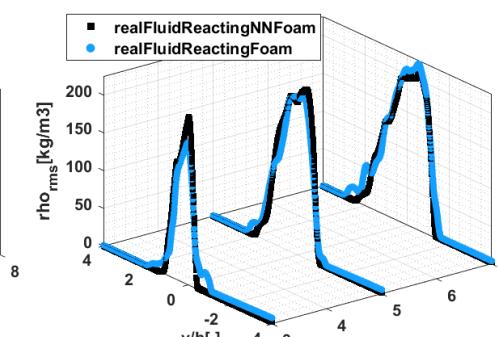
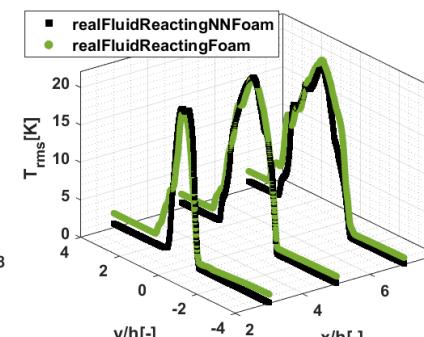
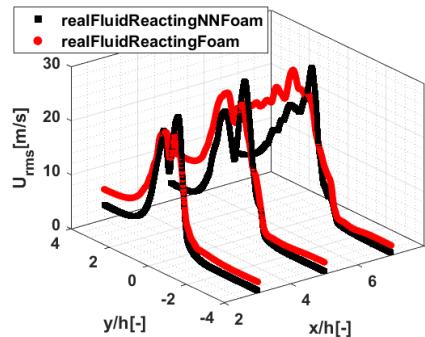
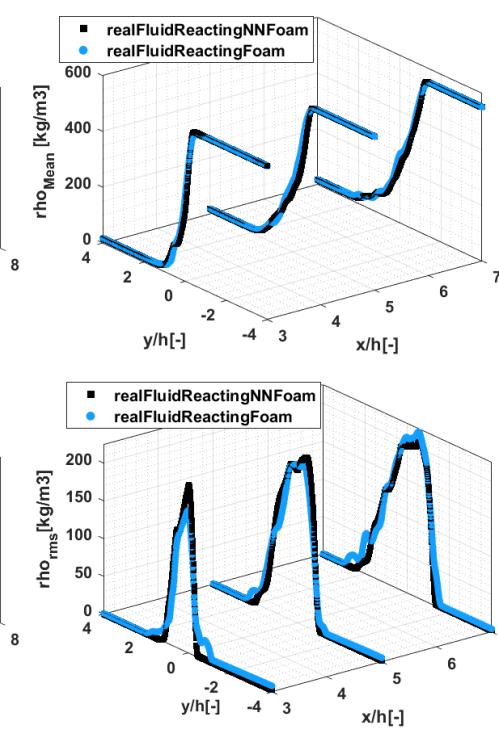
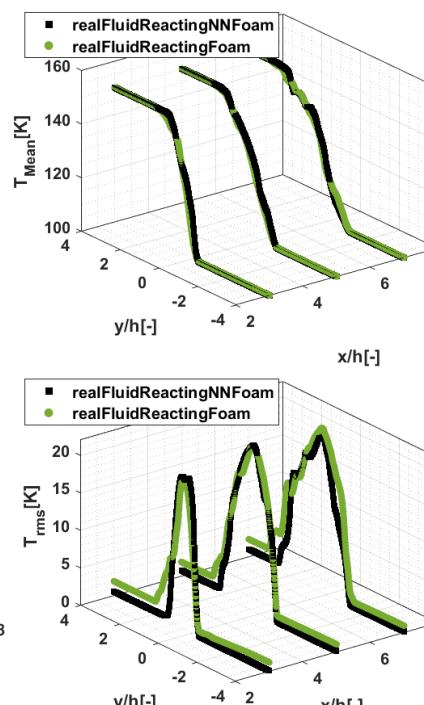
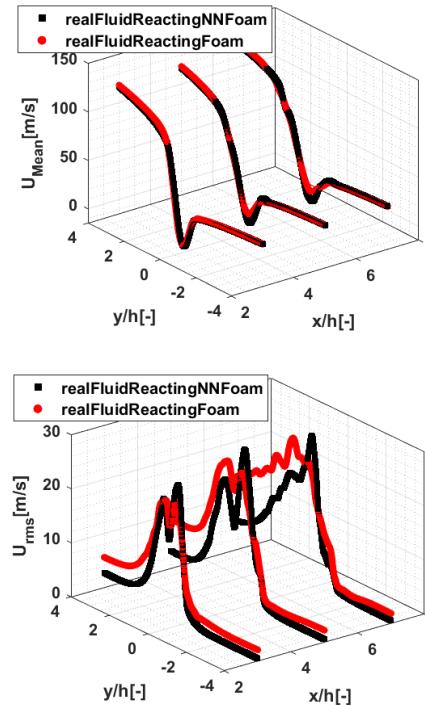
realFluidReactingFoam



GH2-LOX - Results and discussion: fields @ t = 1 ms and time averages



t = 1 ms

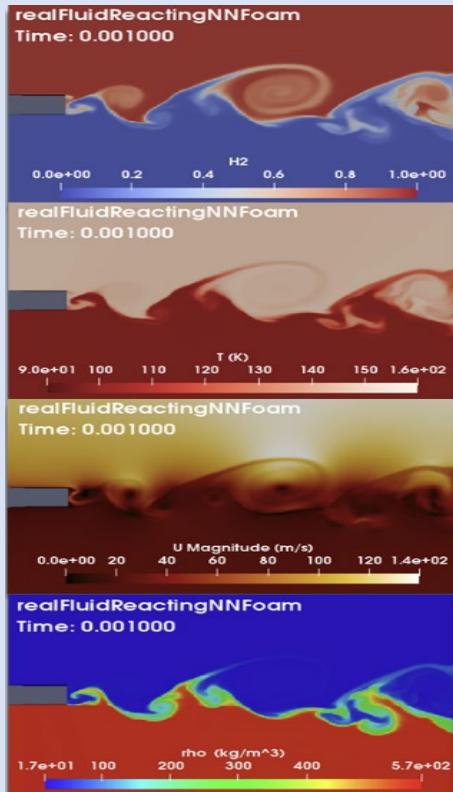


Averages over 4 FTT (1-1.2 ms)

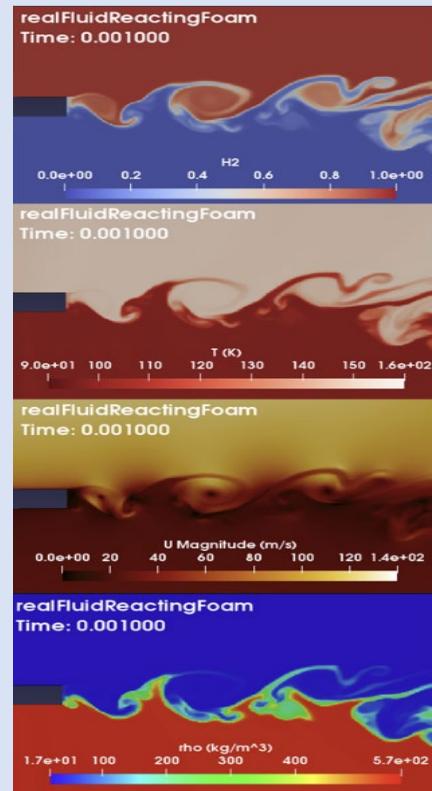
N. Sahranavardfard, D. Aubagnac-Karkar, C. Habchi, G. Costante, F. N. Z. Rahamtamialisoa, and M. Battistoni. "Computation of real-fluid thermophysical properties using a neural network approach implemented in OpenFOAM", Fluids, MDPI, 2024

GH2-LOX - Results and discussion: fields @ t = 1 ms and time averages

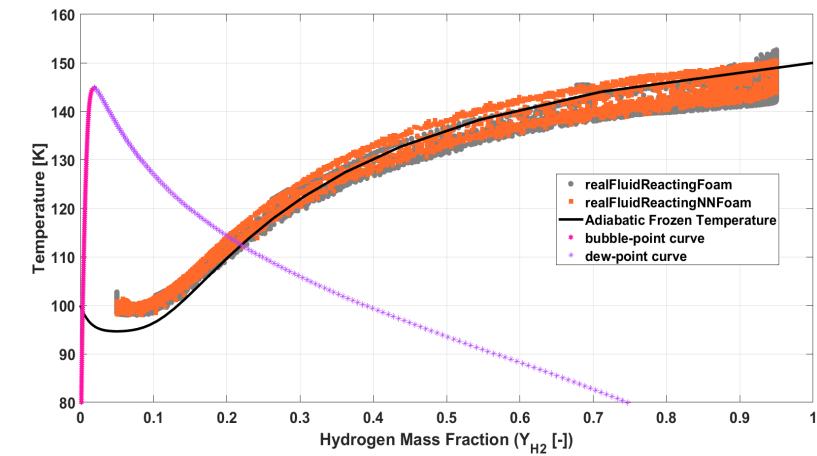
realFluidReactingNNFoam



realFluidReactingFoam



$t = 1 \text{ ms}$



| Solver | Total execution | | | Iteration | |
|-------------------------|-----------------|----------|----------------------------|--------------------|----------|
| | Time (s) | Speed-up | Total number of Iterations | Time/Iter (s/Iter) | Speed-up |
| realFluidReactingFoam | 511096 | 1 | 200550 | 2.548 | 1 |
| realFluidReactingNNFoam | 179317 | 2.850 | 523200 | 0.343 | 7.5 |

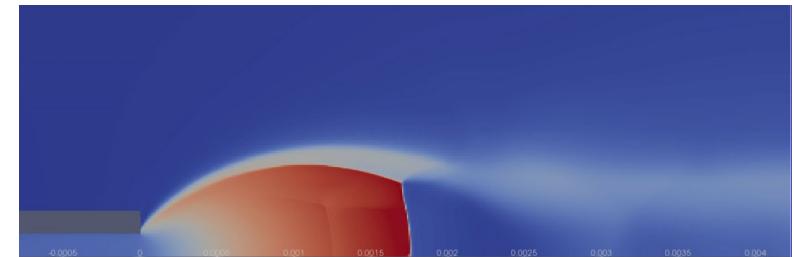
Conclusion: summary and future works

Summary:

- ✓ Exploration of the integration of NN models within the RFM approach for efficiently simulating complex thermodynamic functions in openFoam for a binary mixture under transcritical conditions.
- ✓ realFluidreactingFoam results indicates that the NN model outperforms the original approach in terms of execution time at the same level of accuracy

Future work

- ✓ The study opens avenues for exploring the full potential of ML techniques in addressing complex problems related to multiphase flows also
 - ✓ also with more than just two species
 - ✓ or with other highly-volatile fuels (zero and low carbon fuels)





Michele
Battistoni
Assoc. Professor

Carlo N.
Grimaldi
Full Professor

Jacopo
Zembi
Researcher

Federico
Ricci
Postdoc

Faniiry
Rahantamialisoa
Postdoc

Nasrin
Sahranavardfard
PhD student

Tamara
Gammaidoni
Research Fellow

Filippo
Bittoni
PhD student

Thank you

